PAPER • OPEN ACCESS

Estimation of efficiency of use of water-lifting equipment in technological processes of agricultural production

To cite this article: N A Dotsenko and I V Batsurovska 2022 IOP Conf. Ser.: Earth Environ. Sci. 1049 012047

View the article online for updates and enhancements.

You may also like

- Land use parameters ensuring sustainable development of agricultural producers taking into account characteristics of climatic zones and land quality Yu M Rogatnev, K A Puminova, L V Garafutdinova et al.
- Power law scaling and country-level centralization of global agricultural production and trade
 Marie-Cécile Dupas, José Halloy and Petros Chatzimpiros
- How do countries specialize in agricultural production? A complex network analysis of the global agricultural product space Mercedes Campi, Marco Dueñas and Giorgio Fagiolo



244th Electrochemical Society Meeting

October 8 – 12, 2023 • Gothenburg, Sweden

50 symposia in electrochemistry & solid state science

Abstract submission deadline: **April 7, 2023**

Read the call for papers & submit your abstract!

This content was downloaded from IP address 217.77.211.118 on 08/02/2023 at 12:23

1049 (2022) 012047

Estimation of efficiency of use of water-lifting equipment in technological processes of agricultural production

${\bf N}$ A Dotsenko¹ and I V Batsurovska¹

¹ Mykolayiv National Agrarian University, 9 Georgya Gongadze Str., Mykolayiv, 54020, Ukraine

E-mail: dotsenkona@outlook.com, batsurovska_ilona@outlook.com

Abstract. The article presents the estimation of efficiency of use of water-lifting equipment in technological processes of agricultural production. It is outlined the principle of operation waterlifting equipment in technological processes of agricultural production. It is based on increasing the required pressure for the water supply network by direct repeated use of gravitational forces in the form of weight of the liquid column from natural or artificial pressure. The efficiency of the technological process is assessed by the amount of consumption of water and the speed of flow movement. These parameters (optimization criteria) depend on four main independent factors: the head height; volume of transit tanks; pipe diameter; pipe length. The optimal constructive and technological parameters of water-lifting equipment in technological processes of agricultural production are considered.

1. Introduction

One of the most important problems in the field of agricultural and industrial production is the creation of a modern water supply system. Water supply systems are complex engineering structures that provide both water supply to consumers and drainage and wastewater treatment. The use of water supply systems requires high energy costs, so the creation of systems that will promote energy conservation is necessary for the development of the industry in the country. The water supply system plays an important role in agriculture. The productivity of livestock farms depends on the water supply. To create operational water reserves, water towers are used, the filling of which requires significant energy consumption. Thus, the task of water supply systems is to expand the technological capabilities of the water supply process, increase its reliability, reduce its capital and operating costs, simplify design. Therefore, it is proposed to perform the process of increasing the pressure by gravity in the form of the weight of the liquid column of the required height. To solve it, it is proposed to implement a system of gravity water-lifting equipment that provides an automatic process of reusable pressure, which exists in the system for water supply to the consumer.

An analysis of the technical solutions of the water lift process was performed. In the research were presented the functions of water-lifting aerator technology used in these reservoirs for water quality improvement and its engineering solutions course [1]. The results showed that the technology of water-lifting aerators can effectively control the release of endogenous pollutants, remove volatile contaminants, and reduce the pollution load in reservoirs [2]. Significant

Content from this work may be used under the terms of the Creative Commons Attribution 3.0 licence. Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI. Published under licence by IOP Publishing Ltd 1

opportunities exist to reduce pumping system energy consumption through smart design, retrofitting, and operating practices [3]. The results suggest that a unit increase in the level of farm mechanization increases the demand for hired labour [4]. The authors developed techniques to incorporate differential pressure measurements in flat dilatometer and piezo-penetrometer tests to facilitate in situ measurements under water in a reservoir [5]. Also, hydraulic collecting and pipe transportation are regarded as an efficient way for exploiting submarine mineral resources [6]. The paper presents a comprehensive review of the progress that has been achieved in the past years about cavitation in valves including both mechanical heart valves and control valves [7]. The study investigates the additional installation of a pilot channel running along the canal bottom to constrict the flow width and increase the flow depth [8].

The analytical models of water lifting process in industry were investigated. The paper presents a semi-analytical model that facilitates the optimum design of small-scale hydropower systems [9]. Several practical applications in fluid mechanics have the interest to reduce energy dissipation by reducing the drag or pressure drop [10]. The paper puts forward a formula for the effect of silt sediment on the lifting force [11]. Nevertheless, site-specific factors such as differing discharge conditions, topographical boundary conditions, wastewater volume and composition should be taken into consideration by wastewater practitioners during energy benchmarking assessments [12]. Hydro informatics applies software-based artificial technology for determining these consequences accompanied to water-based approach [13]. The "waterscapes" influence on the administrative geography of the region, which were the locations where these activities took place, and the people in charge of them were integrated within the socio-economic network [14]. Water development, particularly hydropower, provides an important source of renewable energy [15]. Water Engineering Modelling and Mathematic Tools provides an informative resource for practitioners who want to learn more about different techniques and models in water engineering and their practical applications and case studies [16]. The evolution of the major achievements in water lifting devices with emphasis on the major technologies is presented and discussed [17] These technologies are the underpinning of modern achievements in water engineering [18]. The authors investigated some aspects of estimation the processes of quality management system at enterprises [19] and the mathematical modelling of the technology of processing the agricultural production [20] but the estimation of efficiency of use of water-lifting equipment in technological processes of agricultural production was not the specific subject of research.

The aim of the article is to estimate the efficiency of use of water-lifting equipment in technological processes of agricultural production.

2. Methods

Methods of physics, hydraulics, analysis and modelling were used in solving the research tasks. The study of technological parameters of the water-lifting equipment was carried out in the laboratory using the methods of mathematical statistics [21] with data processing on a PC. Experimental studies of the rise of water by water-lifting equipment were carried out on a specially designed installation.

3. Principle of operation water-lifting equipment in technological processes of agricultural production

The principle of operation of equipment for lifting water (figure 1) in technological processes of agricultural production is based on increasing the required pressure for the water supply network by direct repeated use of gravitational forces in the form of weight of the liquid column from natural or artificial pressure. In this case, the natural pressure can be obtained as a result of differences in the height of the water column in waterfalls, rivers, when excess water leaks from ponds and reservoirs, and artificial pressure from any water network in which it is not enough to meet consumer needs.

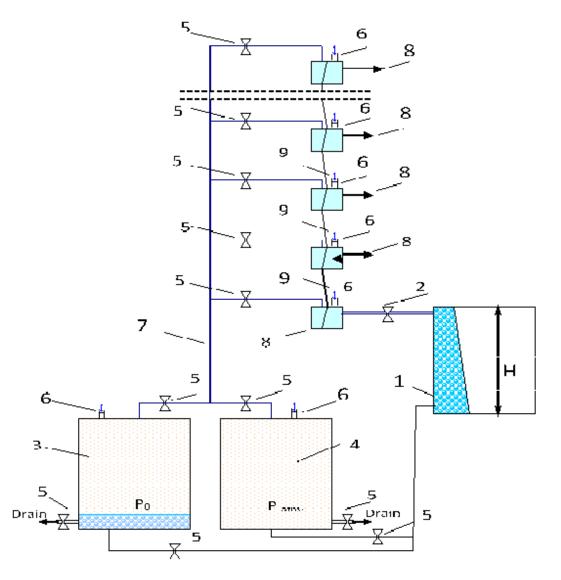


Figure 1. Water-lifting equipment in technological processes of agricultural production: 1 - pressure tank, 2 - tap for filling the transit tank, 3 - right base tank, 4 - left base tank, 5 - ball or screw tap, 6 - valve for sealing or depressurization, 7 - compression air pipe, 8 - transit tanks, 9 - pressure pipelines.

The process of operation of equipment for lifting water in the technological processes of agricultural production is as follows. Through the tap for filling the transit tank 2 with water, from the pressure tank 1, the transit tank 8 is filled with water and sealed with a sealing or depressurizing value 6. At the same time the right base tank 3 is sealed and filled with water through a ball or screw tap 5, creating at the same time in it compressed air pressure $P_o = R_{atm.} + \gamma h$, where γ is the specific weight of water, and h is the height of the water column pressure H. Then through a ball or screw value 5, compressed air from the right base tank 3 enters the compression air pipe 7, and then through the value for sealing or depressurization 6 in the transit tank 8 and fills it, and then repeats the cycle of pushing water from the transit tank 8, that is, after filling it with water, it is also sealed only by means of a value for sealing or depressurization 6. In the next transit tanks, the process of filling and ejecting water

ICSF-2022		IOP Publishing
IOP Conf. Series: Earth and Environmental Science	1049 (2022) 012047	doi:10.1088/1755-1315/1049/1/012047

occurs according to the principle described above. In this case, each capacity of the waterlifting equipment starting with the second, provides at a specific level of its rise the value of water pressure $H = \gamma h$. In order to ensure the continuity of the supply of compressed air in the compression air pipe 7 of the device for raising water provides sequential and synchronous inclusion of two tanks: the right base tank 3 and the left base tank 4.

Thus, the process of increasing the pressure in equipment for lifting water of this type can be implemented not only for water supply, but also to use it to obtain sources of cheap, environmentally friendly energy by creating high-pressure hydropower plants of a wide range of capacities. Such installations can be widely used in agriculture, which, like no other industry, needs autonomous water and energy supply. The introduction of this type of installation requires full automation of the process of increasing the gravitational pressure, which eliminates the presence of human.

For experimental studies, the volumes of transit tanks equal to 1 dm, located at a height of 0.5 m, were accepted, and the choice of volumes for base tanks was made on the condition of reliable compressed air supply system for experimental studies. Experimental studies have shown that the optimum value of water flow in the pipeline corresponds to the speed of its movement is 1.2 m/s, and the time of supply of the initial volume of water to the maximum height of the system under consideration is 45 seconds. Studies have shown that taking into account all local system losses and losses along the length of the pipeline, the efficiency of the gravity water lift system is approximately 98%. During the experimental research, all the processes of sealing and depressurization of transit tanks were carried out manually, using conventional ball valves, because in the laboratory it is difficult to create a complete automation of the process of lifting water.

4. Results

The quality of the technological process is assessed by the amount of water consumption (AC)and speed of flow movement (SM). These parameters (optimization criteria) depend on four main independent factors: the head height -H, m (X_1) ; volume of transit tanks -V, m^3 (X_2) ; pipe diameter -d, m (X_3) ; pipe length -l, m (X_4) . The above independent factors are selected as the main in this technological process by conducting preliminary experiments and their ranking according to the degree of impact on the quality of work. The levels of setting of independent variables (factors) and the range of their variation, adopted during the experiments, are given in table 1.

Levels of variation					
Factors	-1	0	+1	Interval of variation	Dimension
$X_1(H)$	3	6	9	3	m
$X_2(V)$	2	4	6	2	m^3
$X_3(d)$	0.02	0.04	0.06	0.02	m
$X_4(l)$	3	6	9	3	m

Table 1. Levels and range of variation factors.

The plan, the average value of AC, SM was calculated. Mathematical models are obtained that adequately describe the The frequency of experiments on each of the optimization criteria was three times. For each line of technological process. The regression equations are:

IOP Conf. Series: Earth and Environmental Science 1049 (2022) 012047

$$AC = 12.5 + 0.58X_1 + 5.4X_2 + 2.1X_3 - 2.6X_4 + 0.63X_1X_2 - 0.6X_1X_3 - 1.3X_1X_4 - -2.8X_2X_3 - 1.06X_2X_4 + 1.5X_3X_4 + 2.1X_1^2 - 5.4X_2^2 - 1X_3^2 + 1.8X_4^2$$
(1)

• for the speed of movement:

$$SM = 0.83 - 0.025X_1 - 0.017X_2 + 0.020X_3 - 0.011X_4 - 0.012X_1X_2 + 0.0056X_1X_3 - 0.042X_1X_4 + 0.048X_2X_3 - 0.013X_2X_4 + 0.0097X_3X_4 + 0.12X_1^2 - (2) - 0.09X_2^2 - 0.012X_3^2 + 0.014X_4^2$$

The analysis of regression equations obtained after statistical processing is usually performed with coded values of factors [21]. The study of the behaviour of optimization criteria depending on the change of independent factors will be carried out using the method of two-dimensional sections.

When substituting $X_3 = 0$ and $X_4 = 0$, the regression equations will look like:

$$AC = 12.5 + 0.58X_1 + 5.4X_2 + 0.63X_1X_2 + 2.1X_1^2 - 5.4X_2^2$$
(3)

$$SM = 0.83 - 0.025X_1 - 0.017X_2 - 0.012X_1X_2 + 0.12X_1^2 - 0.09X_2^2$$
(4)

• for the amount of consumption:

$$AC - 17.218 = 2.183X_1^2 - 5.493X_2^2;$$

• for the speed of movement:

$$SM - 0.8 = 0.119X_1^2 - 0.093X_2^2;$$

The two-dimensional cross section of the response surfaces is shown in figure 2. Consistently fixing the other two factors at level 0 and performing calculations similar to the above, it is obtained the regression equation in the usual form with a new combination of factors.

When substituting $X_1 = 0$ and $X_2 = 0$, the regression equations:

• for the amount of consumption:

$$AC = 12.5 + 2.1X_3 - 2.6X_4 + 1.5X_3X_4 - 1X_3^2 + 1.8X_4^2$$
(5)

• for the speed of movement:

$$SM = 0.83 + 0.020X_3 - 0.011X_4 - 0.0097X_3X_4 - 0.012X_3^2 + 0.014X_4^2$$
(6)

In accordance:

- for the amount of consumption: $X_3 = -1.23$; $X_4 = 0.27$;
- for the speed of movement: $X_3 = -1.153$; $X_4 = 0.795$;

The regression equations in canonical form will take the form:

$$AC - 11.10 = 2.0032X_3^2 - 1.153X_4^2;$$

1049 (2022) 012047

doi:10.1088/1755-1315/1049/1/012047

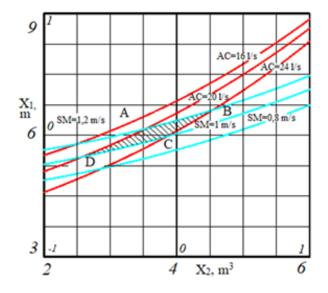


Figure 2. Two-dimensional intersection of response surfaces at $X_3 = 0$ and $X_4 = 0$.

• for the speed of movement:

$$SM - 0.83 = 0.0179X_3^2 + 0.0805X_4^2$$
.

When setting $X_2 = 0$ and $X_4 = 0$, the regression equations have the form:

• for the amount of consumption:

$$AC = 12.5 + 0.58X_1 + 2.1X_3 - 0.6X_1X_3 + 2.1X_1^2 - 1X_3^2$$
(7)

• for the speed of movement:

$$SM = 0.83 - 0.025X_1 + 0.020X_3 + 0.0056X_1X_3 + 0.12X_1^2 - 0.012X_3^2$$
(8)

In accordance:

- for the amount of consumption: $X_1 = -0.427$; $X_3 = -0.96$;
- for the speed of movement: $X_1 = 0.084; X_3 = 0.852;$

Regression equation in canonical form:

• for the amount of consumption:

$$AC - 12.5 = 2.2X_1^2 - 1.035X_3^2;$$

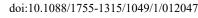
• for the speed of movement:

$$SM - 0.94 = 0.12X_1^2 - 0.0121X_3^2.$$

The two-dimensional cross section of the response surfaces is shown in figure 3. When setting $X_1 = 0$ and $X_3 = 0$, the regression equations have the form:

$$AC = 12.5 + 5.4X_2 - 2.6X_4 - 1.06X_2X_4 - 5.4X_2^2 + 1.8X_4^2$$
(9)

1049 (2022) 012047



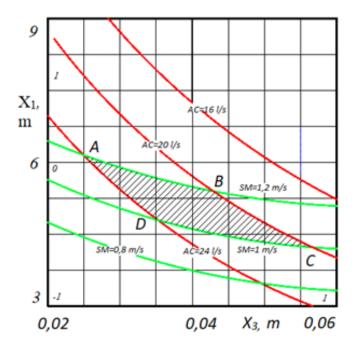


Figure 3. Two-dimensional intersection of response surfaces at $X_2 = 0$ and $X_4 = 0$.

• for the speed of movement:

$$SM = 0.83 - 0.017X_2 - 0.011X_4 - 0.013X_2X_4 - 0.09X_2^2 + 0.014X_4^2$$
(10)

In accordance:

- for the amount of consumption: $X_2 = 0.41$; $X_4 = 0.841$;
- for the speed of movement: $X_2 = -0.121; X_4 = 0.336;$

Regression equation in canonical form:

• for the amount of consumption:

$$AC - 10.67 = 1.894X_2^2 - 5.51X_4^2;$$

• for the speed of movement:

$$SM - 0.709 = 0.0144X_2^2 - 0.0904X_4^2.$$

When setting $X_2 = 0$ and $X_3 = 0$, the regression equations have the form:

• for the amount of consumption:

$$AC = 12.5 + 0.58X_1 - 2.6X_4 - 1.3X_1X_4 + 2.1X_1^2 + 1.8X_4^2$$
(11)

• for the speed of movement:

$$SM = 0.83 - 0.025X_1 - 0.011X_4 - 0.042X_1X_4 + 0.12X_1^2 + 0.014X_4^2$$
(12)

In accordance:

• for the amount of consumption: $X_1 = 0.098$; $X_4 = 0.757$;

IOP Conf. Series: Earth and Environmental Science 1049 (2022) 012047

- for the speed of movement: $X_1 = 0.235; X_4 = 0.74;$
- Regression equation in canonical form:
- for the amount of consumption

$$AC - 12.21 = 2.69X_1^2 + 1.32X_4^2;$$

• for the speed of movement:

$$SM - 0.87 = 0.12X_1^2 + 0.0099X_4^2.$$

The two-dimensional cross section of the response surfaces is shown in figure 4.

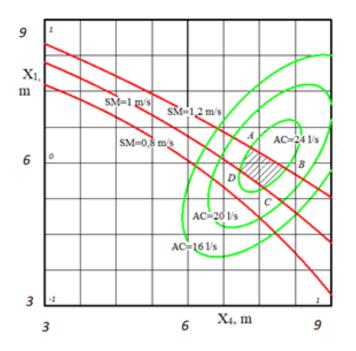


Figure 4. Two-dimensional cross-section of the response surfaces at $X_2 = 0$ and $X_3 = 0$.

When setting $X_1 = 0$ and $X_4 = 0$, the regression equations have the form:

• for the amount of consumption:

$$AC = 12.5 + 5.4X_2 + 2.1X_3 - 2.8X_2X_3 - 5.4X_2^2 - 1X_3^2$$
(13)

• for the speed of movement:

$$SM = 0.83 - 0.017X_2 + 0.020X_3 + 0.048X_2X_3 - 0.09X_2^2 - 0.012X_3^2$$
(14)

In accordance:

- for the amount of consumption: $X_2 = 1.225$; $X_3 = -2.71$;
- for the speed of movement: $X_2 = 0.273; X_3 = 1.38;$

Regression equation in canonical form:

$$AC - 12.86 = -0.58X_2^2 - 5.89X_3^2;$$

1049 (2022) 012047

- for the speed of movement:
 - $SM 0.78 = -0.0052X_2^2 0.0968X_3^2.$

After the analysis of two-dimensional surfaces of section (figures 2–4) it is possible to make the following statements. With the value of the existing pressure equal to 5.5 - 6.5 m and the volume of transit tanks equal to 3 - 4.5 m³, the amount of consumption of water will be in the range of 20 - 24 l/s, and the speed of flow movement will be 1 - 1.2 m/s (figure is limited by ABCD points, figure 2). The diameter of the pipeline will be 0.04 m, the length of the pipeline will be 6 m. Moreover, with increasing pressure increases the amount of flow, the speed also increases. And if increases the volume of transit tanks, the speed of movement begins to increase, but the amount of consumption decreases. At the existing pressure equal to 4.5 - 6 m and the diameter of the pipeline, which is 0.025 - 0.055 m, the amount of consumption of water will be within 20 - 24 l/s, the speed of flow movement will be 1.2 m/s. The volume of transit tanks will be 4 m³, with a pipeline length of 6 m (figure ABCD, figure 3). Moreover, increasing the diameter of the pipeline, the flow rate increases, and the speed begins to decline.

At the level of the existing pressure within 6-6.5 m and length of the pipeline equal 7-8 m, the amount of consumption of water will be 24 l/s, at speed of flow movement within 1-1.2 m/s (figure ABCD, figure 4). Moreover, the diameter of the pipeline will be 0.04 m, with the volume of transit tanks equal to 4 m. But with increasing length of the pipeline, the flow rate and speed decrease.

The optimal constructive and technological parameters of water-lifting equipment can be considered as follows: the head height $X_1 = 5...6.5$ m; volume of transit tanks $X_2 = 4...4.5$ m³; diameter of the pipeline $X_3 = 0.04...0.05$ m; the length of the pipeline $X_4 = 6...7$ m. The optimization criteria are in the range: the amount of consumption of water AC = 20 - 24 l/s; the speed of flow movement SM = 1 - 1.2 m/s.

5. Conclusion

A review of literature sources on the use of systems and equipment for water supply showed that the known technical solutions for raising water in water bodies usually have low efficiency and require energy consumption during operation. Also, they are not always technological in addressing the issues of increasing the pressure in the water supply network and maintaining it at the level necessary for the consumer. Thus, there is a need to address the issue of improving the quality of water supply to consumers, reducing energy consumption in the operation of the water supply system and maintaining the required pressure in the water supply network by designing water-lifting equipment in technological processes of agricultural production. It was found that the main optimization criteria for assessing the quality of the technological process were: the amount of consumption of water AC = 20 - 24 l/s and the speed of flow movement SM = 1 - 1.2 m/s.

On the basis of theoretical and experimental studies it is established that these optimization criteria depend on four main independent factors: the head height – H, m; volume of transit tanks – V, m; pipe diameter – d, m; pipe length – l, m. Also, the most favourable constructive and technological parameters of the water-lifting equipment are established, namely: head height $X_1 = 5...6.5$ m; volume of transit tanks $X_2 = 4...4.5$ m³; diameter of the pipeline $X_3 = 0.04...0.05$ m; the length of the pipeline $X_4 = 6...7$ m.

ORCID iDs

N A Dotsenko https://orcid.org/0000-0003-1050-8193 I V Batsurovska https://orcid.org/0000-0002-8407-4984

doi:10.1088/1755-1315/1049/1/012047

References

- Huang T (ed) 2015 Water Pollution and Water Quality Control of Selected Chinese Reservoir Basins (The Handbook of Environmental Chemistry vol 38) (Cham: Springer International Publishing) URL https://doi.org/10.1007/978-3-319-20391-1
- Huang T, Li X, Ma W and Cong H 2016 Water quality improvement by water-lifting aerators Water Pollution and Water Quality Control of Selected Chinese Reservoir Basins (The Handbook of Environmental Chemistry vol 38) ed Huang T (Cham: Springer International Publishing) pp 347-384 ISBN 978-3-319-20391-1 URL https://doi.org/10.1007/978-3-319-20391-1_11
- [3] Ali M H 2011 Irrigation system designing Practices of Irrigation & On-farm Water Management: Volume 2 (New York, NY: Springer New York) pp 65–110 ISBN 978-1-4419-7637-6 URL https://doi.org/10. 1007/978-1-4419-7637-6_3
- [4] Rajkhowa P and Kubik Z 2021 Indian Economic Review 56 487-513 ISSN 2520-1778 URL https://doi. org/10.1007/s41775-021-00120-x
- [5] Lee J T, Wang C C, Ho Y T and Huang A B 2013 Acta Geotechnica 8 373–380 ISSN 1861-1133 URL https://doi.org/10.1007/s11440-012-0188-1
- [6] Zhang Y, Lu X, Zhang X, Chen Y, Xiong H and Zhang L 2021 Acta Mechanica Sinica 37 613–619 ISSN 1614-3116 URL https://doi.org/10.1007/s10409-020-01022-6
- [7] Qian J y, Gao Z x, Hou C w and Jin Z j 2019 Bio-Design and Manufacturing 2 119–136 ISSN 2522-8552 URL https://doi.org/10.1007/s42242-019-00040-z
- [8] Lindenschmidt K E and Carstensen D 2015 Österreichische Wasser- und Abfallwirtschaft 67 230–239 ISSN 1613-7566 URL https://doi.org/10.1007/s00506-015-0235-x
- [9] Aryal R, Dokou Z, Malla R B and Bagtzoglou A C 2020 Structural and Multidisciplinary Optimization 61 1303-1318 ISSN 1615-1488 URL https://doi.org/10.1007/s00158-019-02416-2
- [10] Katsuno E T, Dantas J L D and Silva E C N 2020 Structural and Multidisciplinary Optimization 62 2915–2933 ISSN 1615-1488 URL https://doi.org/10.1007/s00158-020-02706-0
- [11] Gao S, Xu G and Wang M 2015 Transactions of Tianjin University 21 50-55 ISSN 1995-8196 URL https://doi.org/10.1007/s12209-015-2304-4
- [12] Clos I, Krampe J, Alvarez-Gaitan J P, Saint C P and Short M D 2020 Water Conservation Science and Engineering 5 115–136 ISSN 2364-5687 URL https://doi.org/10.1007/s41101-020-00086-6
- [13] Roy U 2017 Water Conservation Science and Engineering 2 145-152 ISSN 2364-5687 URL https://doi. org/10.1007/s41101-017-0035-1
- [14] Borrelli N 2020 Water History 12 39-55 ISSN 1877-7244 URL https://doi.org/10.1007/ s12685-020-00241-9
- [15] Tian F, Wu B, Zeng H, Ahmed S, Yan N, White I, Zhang M and Stein A 2020 Water Resources Management 34 1725–1741 ISSN 1573-1650 URL https://doi.org/10.1007/s11269-020-02524-5
- [16] Peters R W 2011 Environmental Progress & Sustainable Energy 30 266-267 URL https://doi.org/10.
 1002/ep.10602
- [17] Cheremisinoff N P 2001 Handbook of Water and Wastewater Treatment Technologies (Butterworth-Heinemann) ISBN 978-0-7506-7498-0
- [18] Yannopoulos S I, Lyberatos G, Theodossiou N, Li W, Valipour M, Tamburrino A and Angelakis A N 2015 Water 7 5031–5060 ISSN 2073-4441 URL https://doi.org/10.3390/w7095031
- [19] Trisch R, Gorbenko E, Dotsenko N, Kim N and Kiporenko G 2016 Eastern-European Journal of Enterprise Technologies 4 18–24 URL https://doi.org/10.15587/1729-4061.2016.75503
- [20] Shebanin V, Atamanyuk I, Gorbenko O, Kondratenko Y and Dotsenko N 2019 Food Science and Technology 13 118–126
- Bortz J and Schuster C 2010 Statistik für Human- und Sozialwissenschaftler 7th ed Springer-Lehrbuch (Heidelberg: Springer Berlin) URL https://doi.org/10.17877/DE290R-6043